



HITS

Heidelberg Institute for
Theoretical Studies



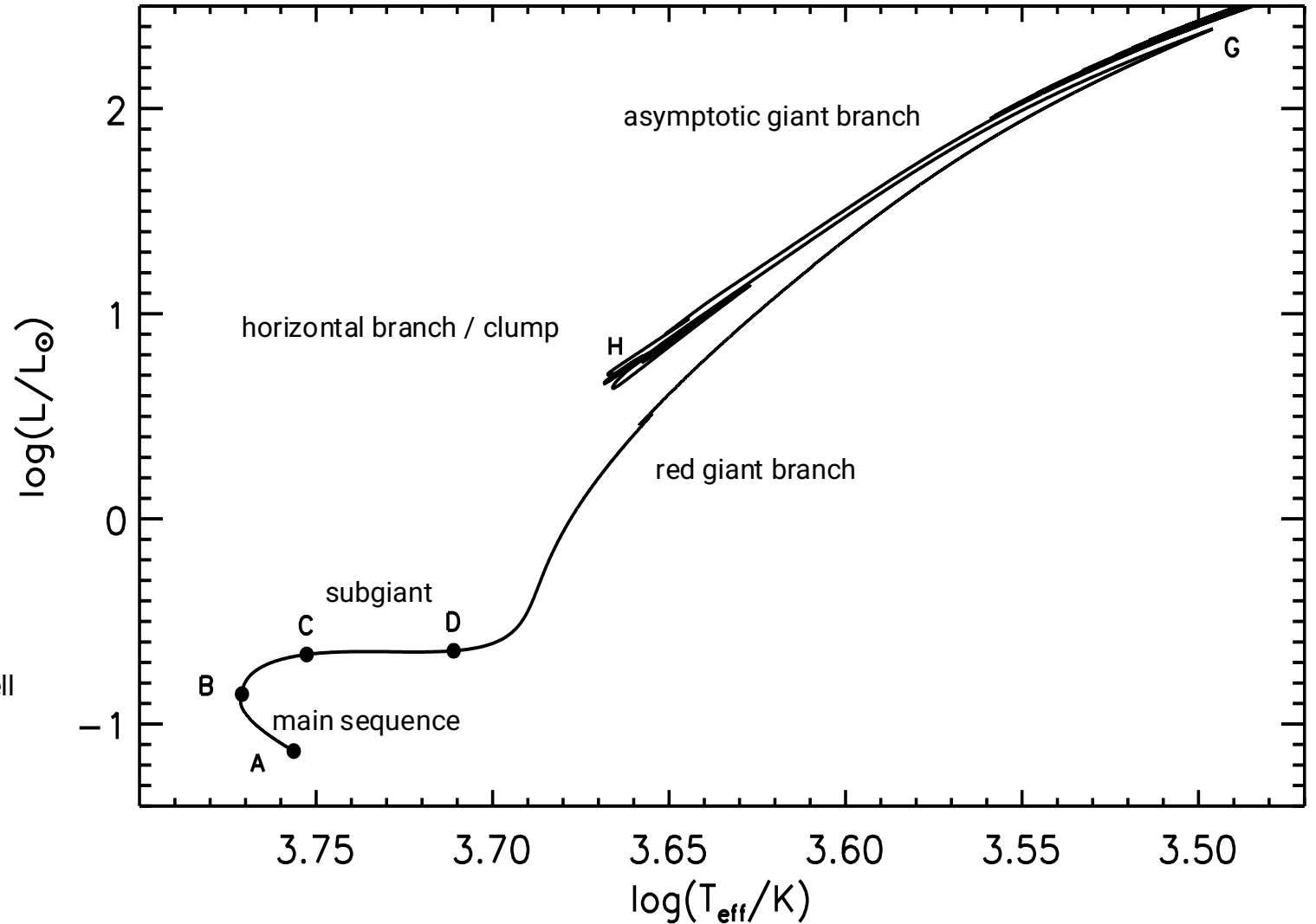
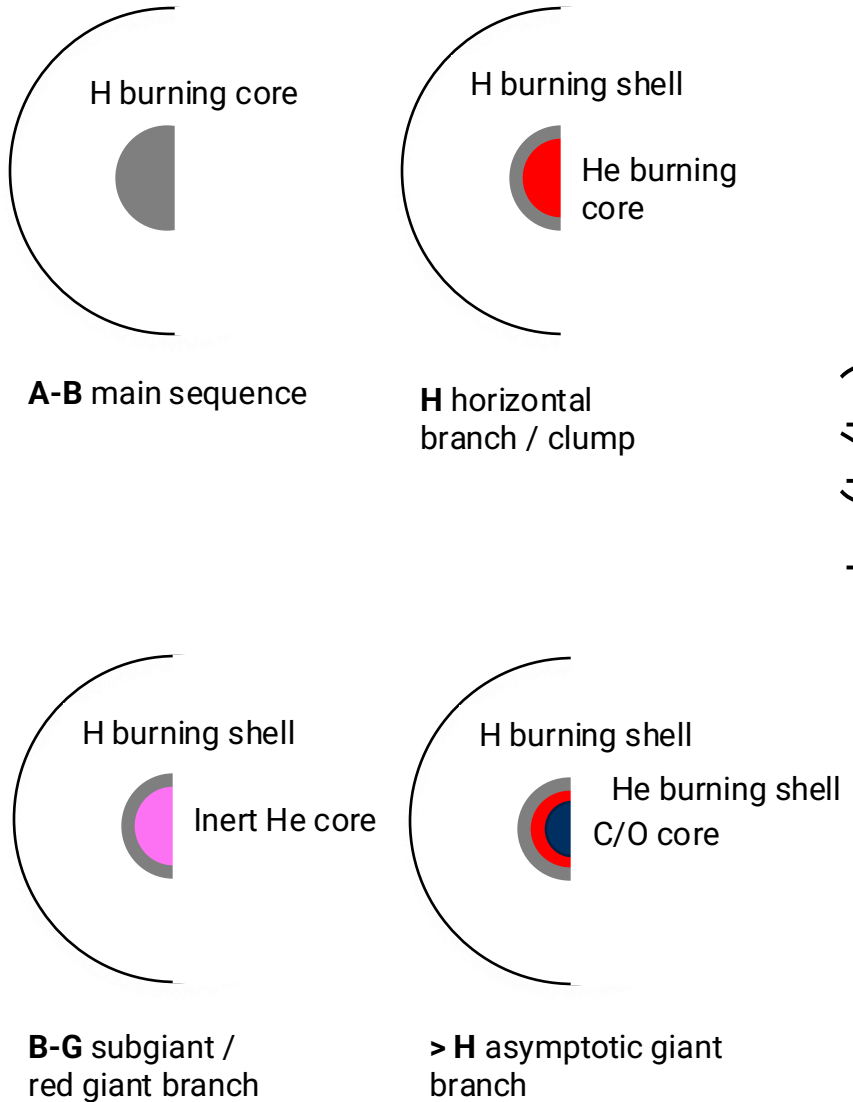
The quest for the ultimate stellar model

Red giants

Saskia Hekker

TAs: Susmita Das; Noi Shitrit; Arthur Le Saux; Zhao Guo

Stellar Structure & Evolution



A&A, 683, A189 (2024)

<https://doi.org/10.1051/0004-6361/202348276>

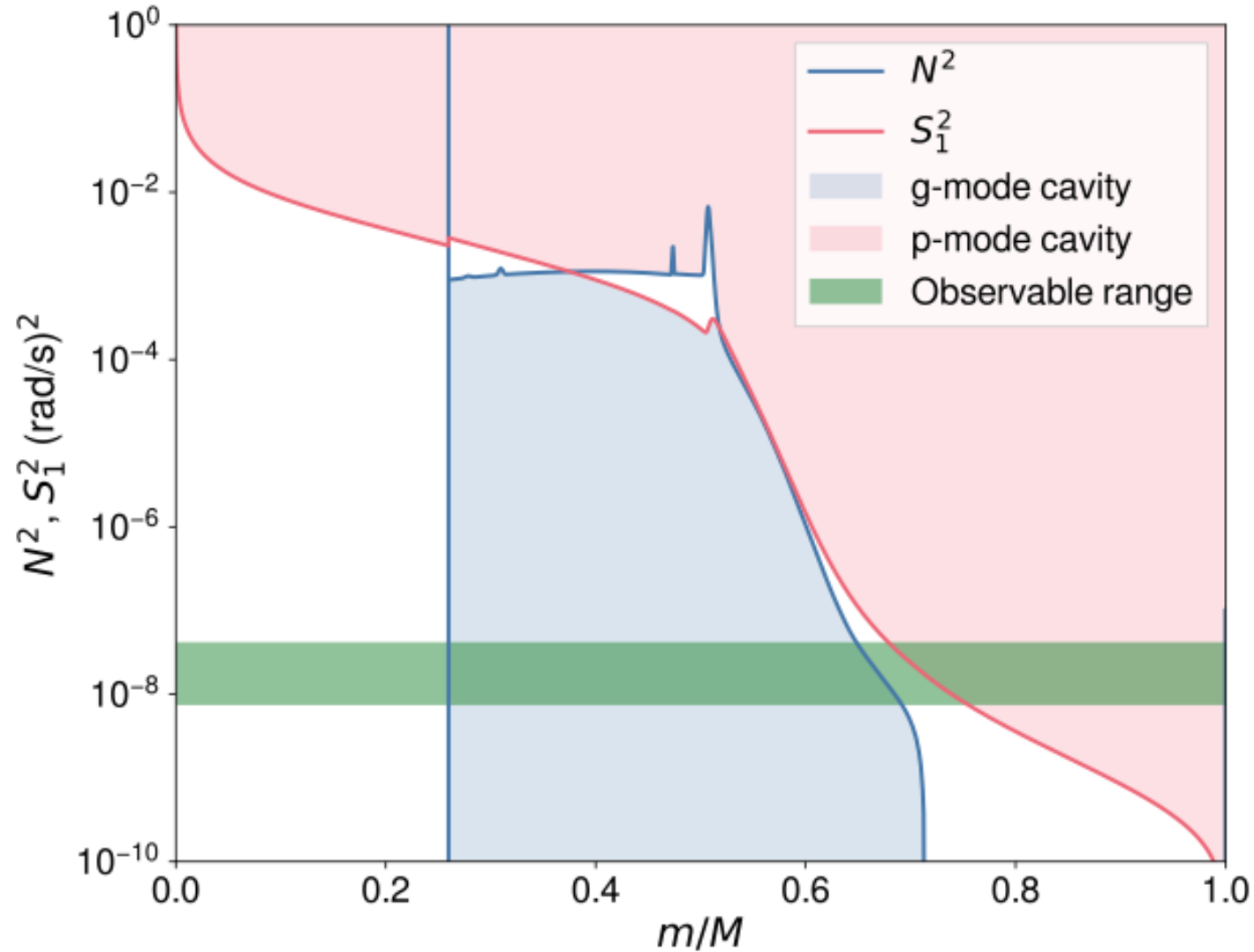
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**Astronomy
&
Astrophysics**

Effect of nuclear reactions rates and core boundary mixing on the seismology of red clump stars

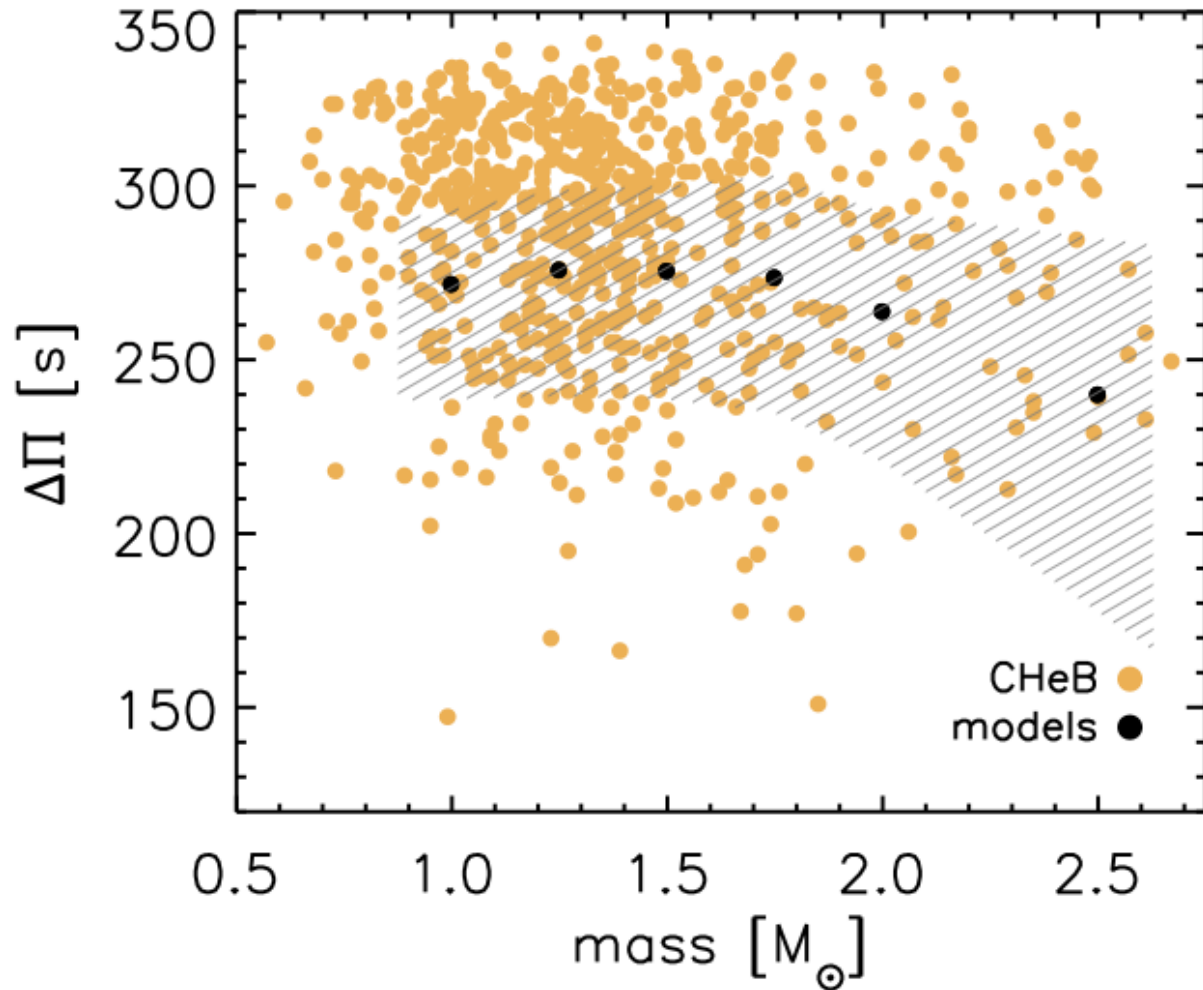
Anthony Noll¹, Sarbani Basu², and Saskia Hekker^{1,3}

Core helium burning stars



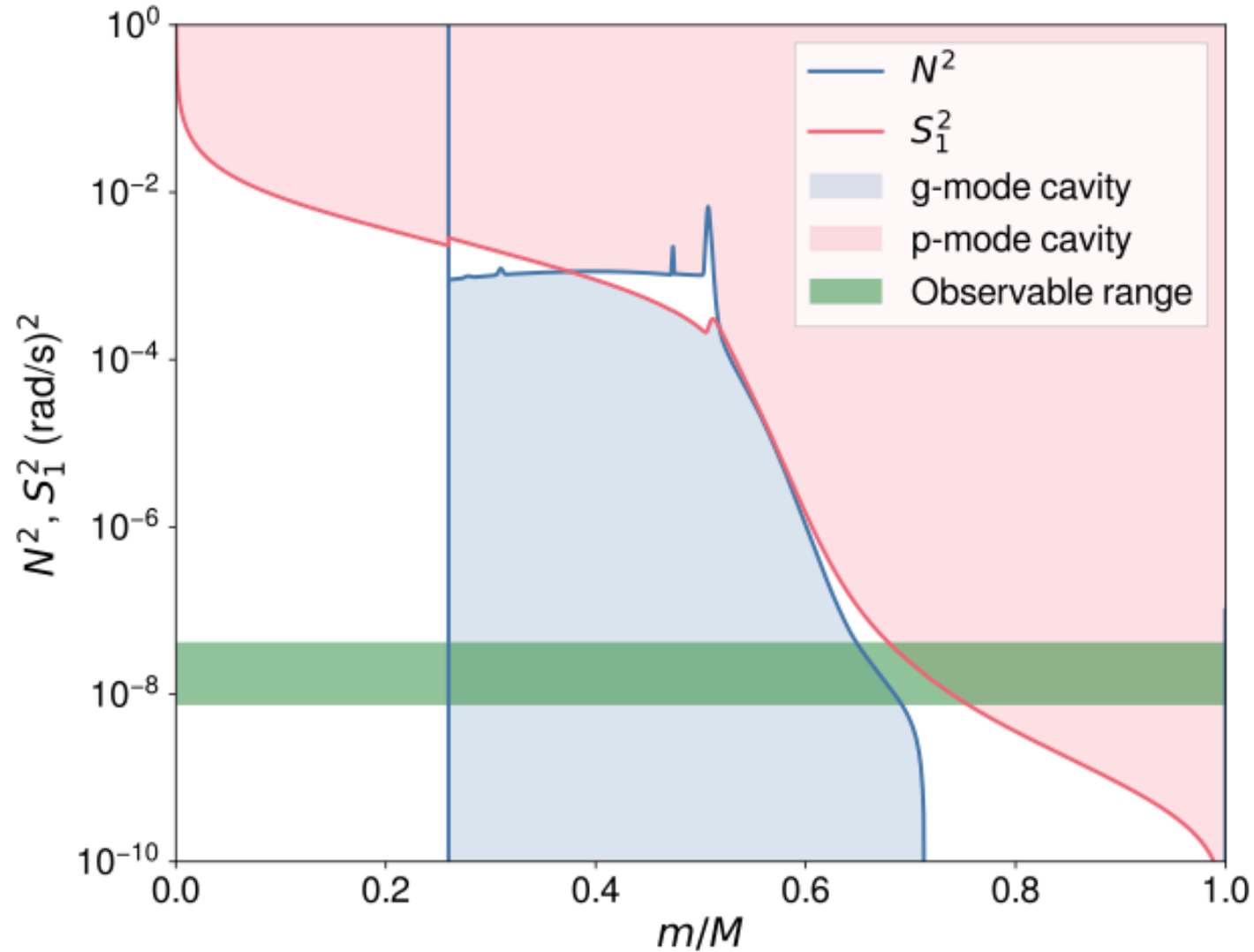
$$\Delta\Pi_\ell = \frac{2\pi^2}{\sqrt{\ell(\ell+1)}} \left(\int_{r_0}^{r_1} \frac{N}{r} dr \right)^{-1}$$

Core helium burning stars



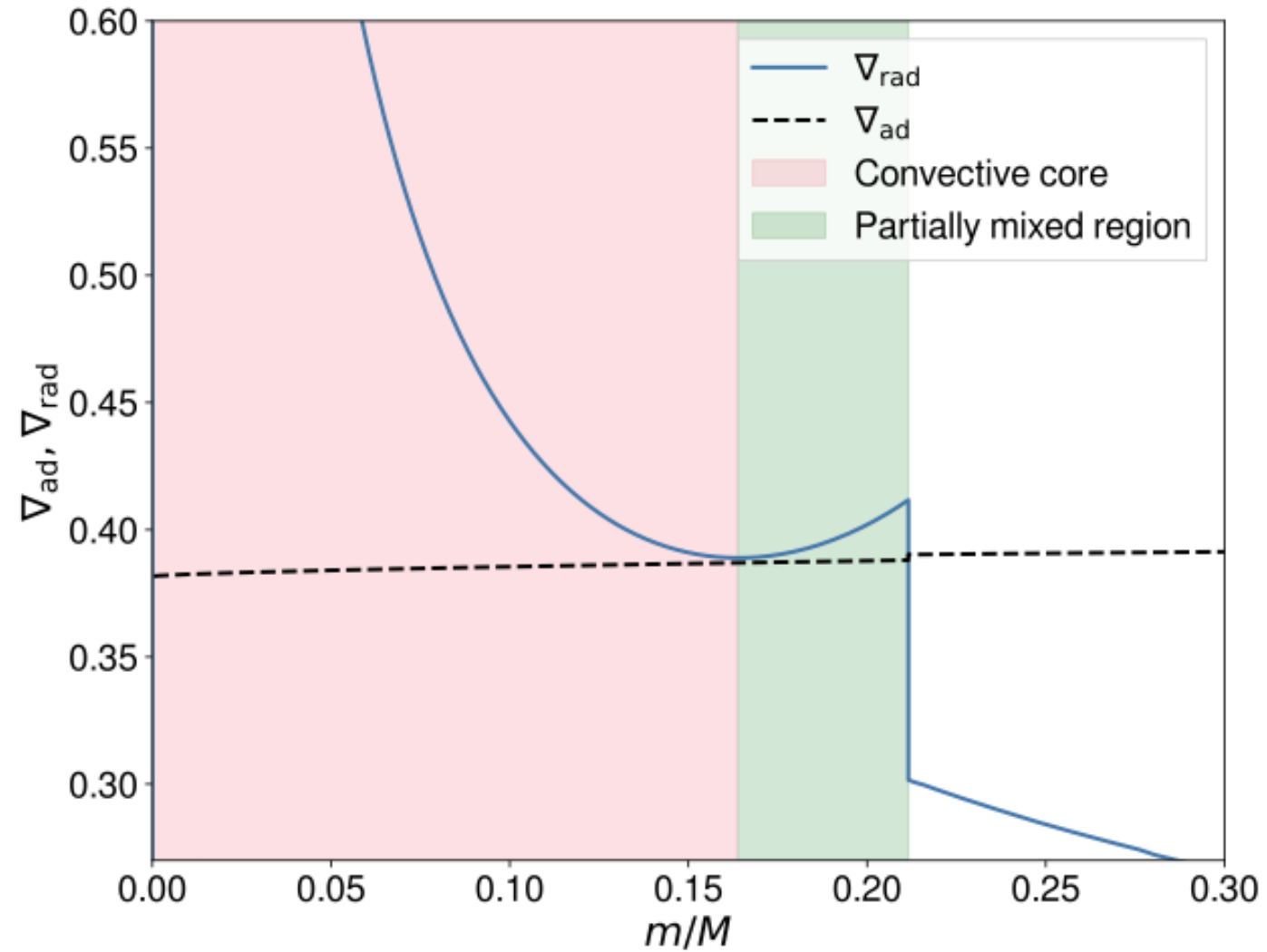
Range in $\Delta\Pi$ NOT matched
by models with canonical
physics!

Core helium burning stars



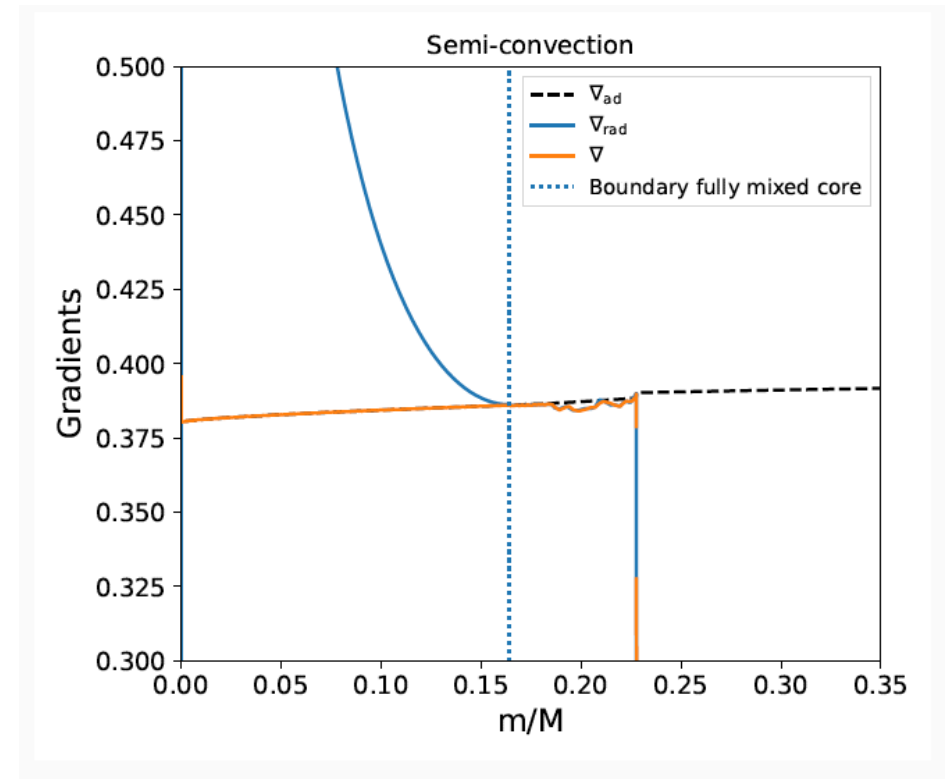
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Core boundary mixing



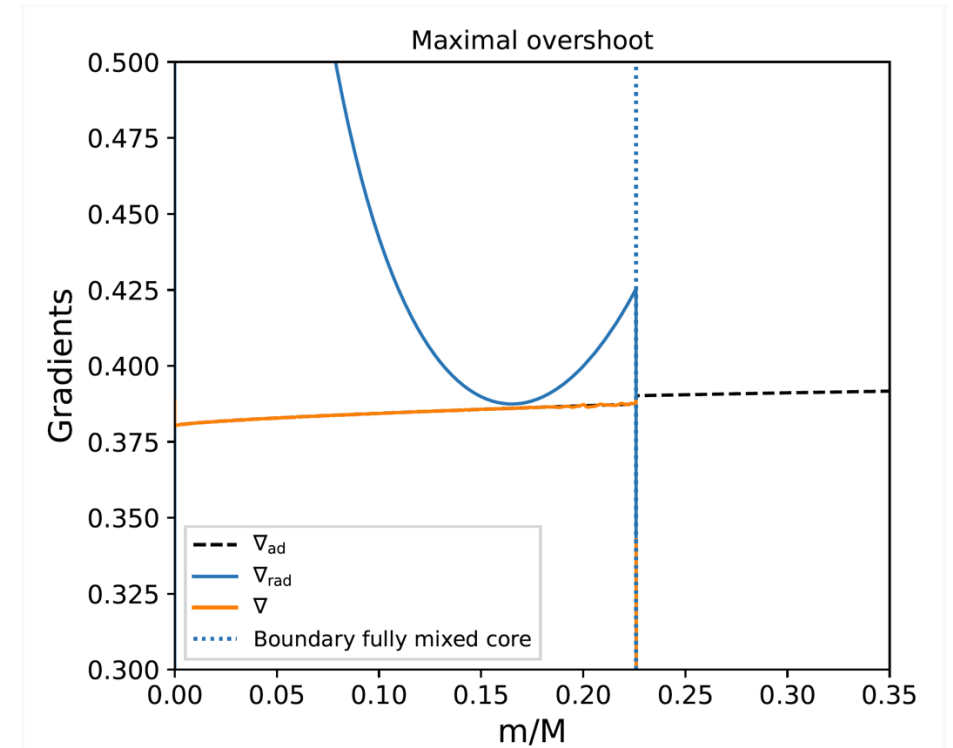
Core boundary mixing: different prescriptions

- semi convection: partially mixed region is buoyantly neutral, i.e. $\nabla_{\text{rad}} = \nabla_{\text{ad}}$



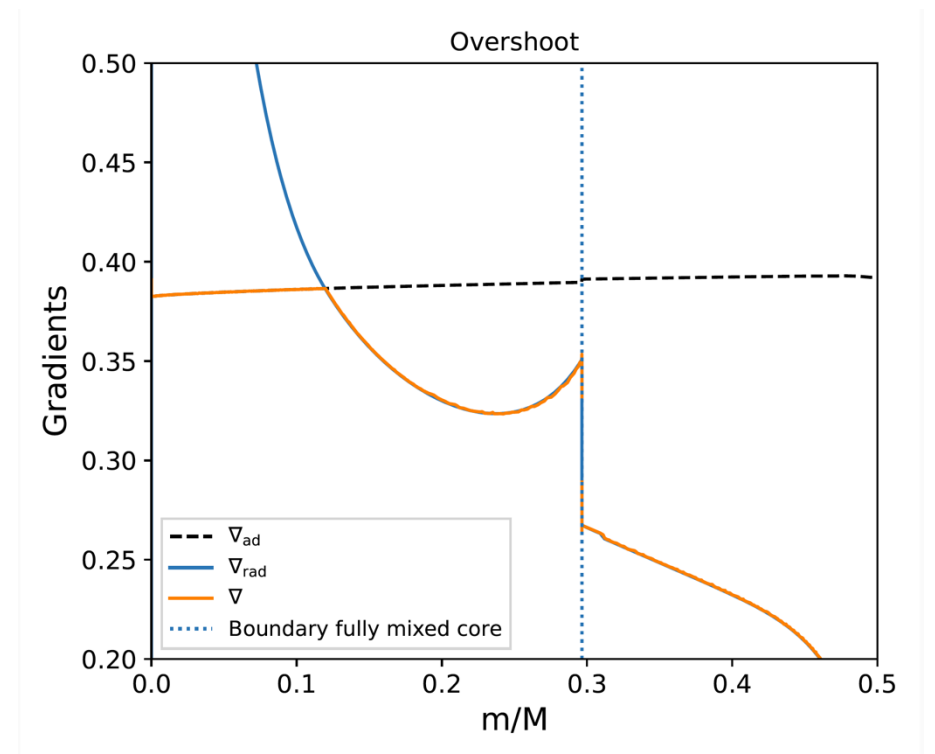
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- maximal overshoot: largest core possible by including the 'partially mixed region'



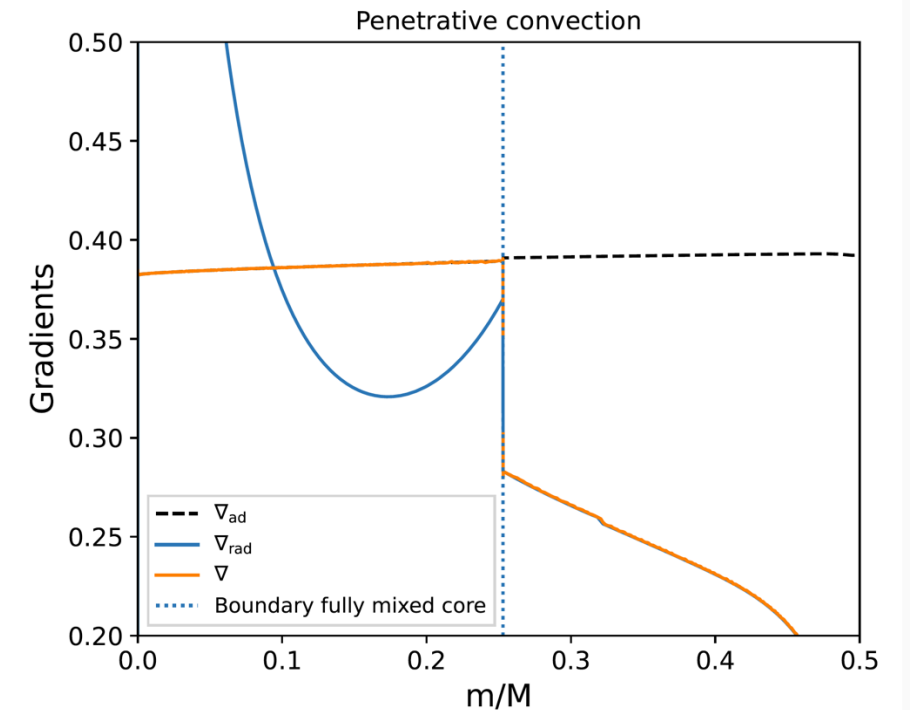
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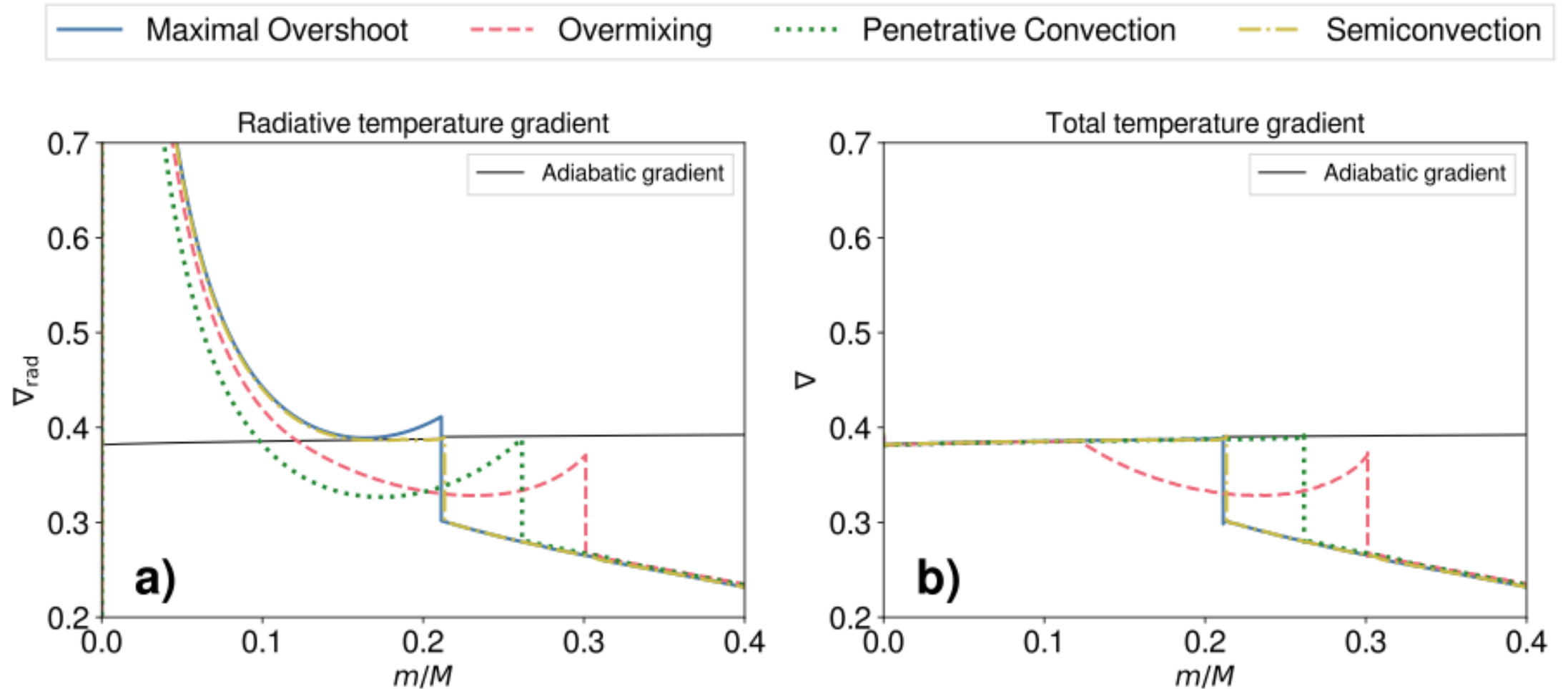


Core boundary mixing: different prescriptions

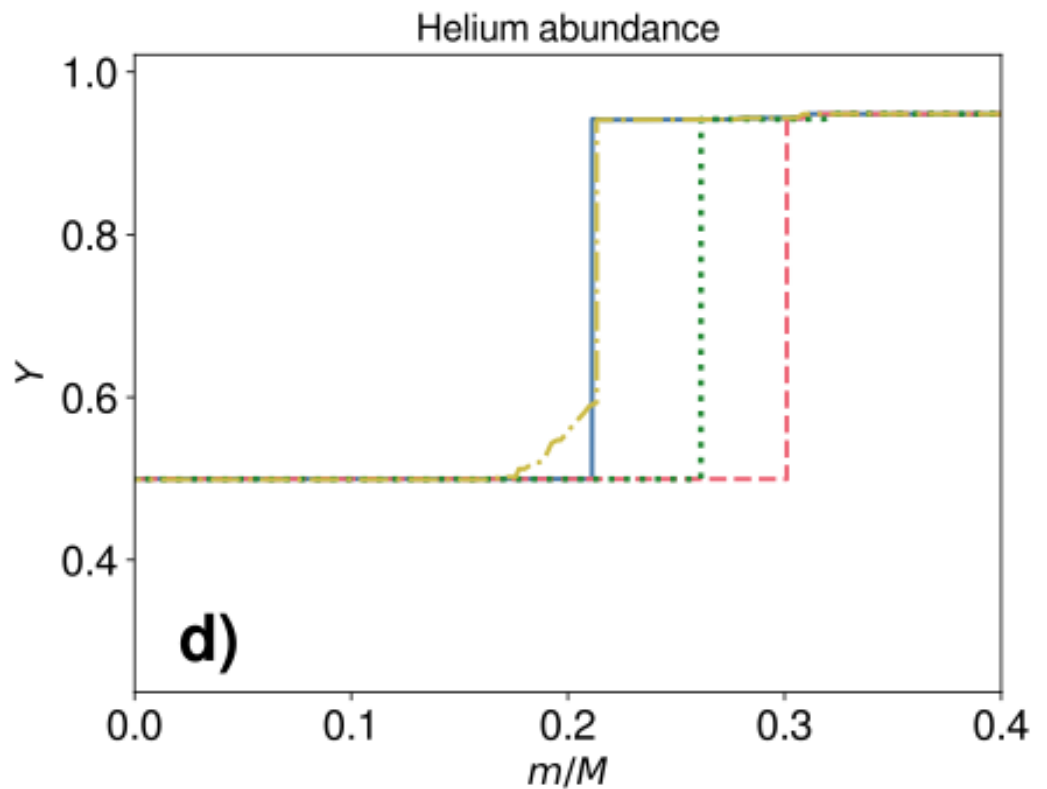
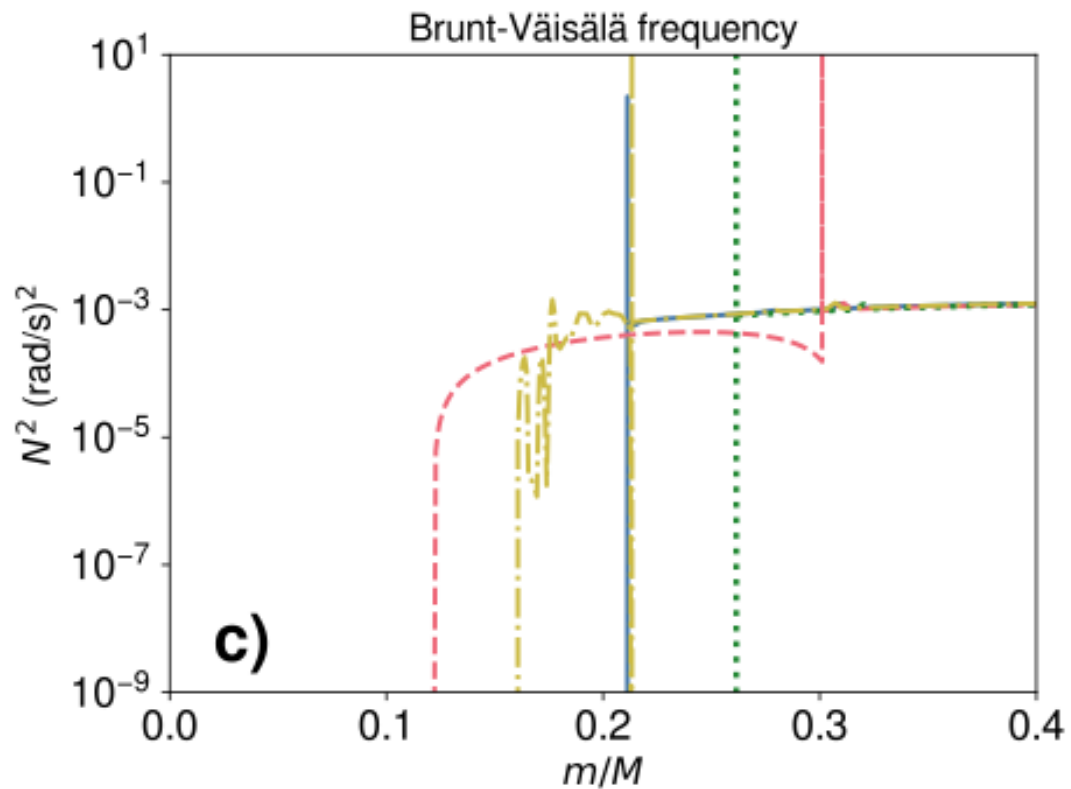
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- penetrative convection: overshoot with $d_{ov} = \alpha_{ov} H_p$ and thermal stratification in extended region adiabatic ($\nabla = \nabla_{\text{ad}}$)



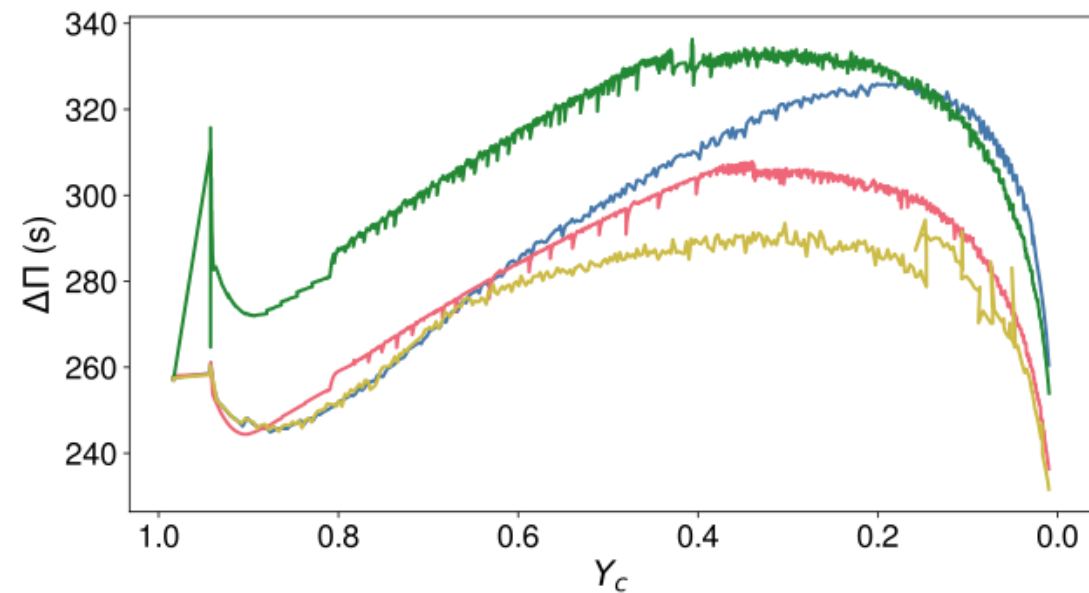
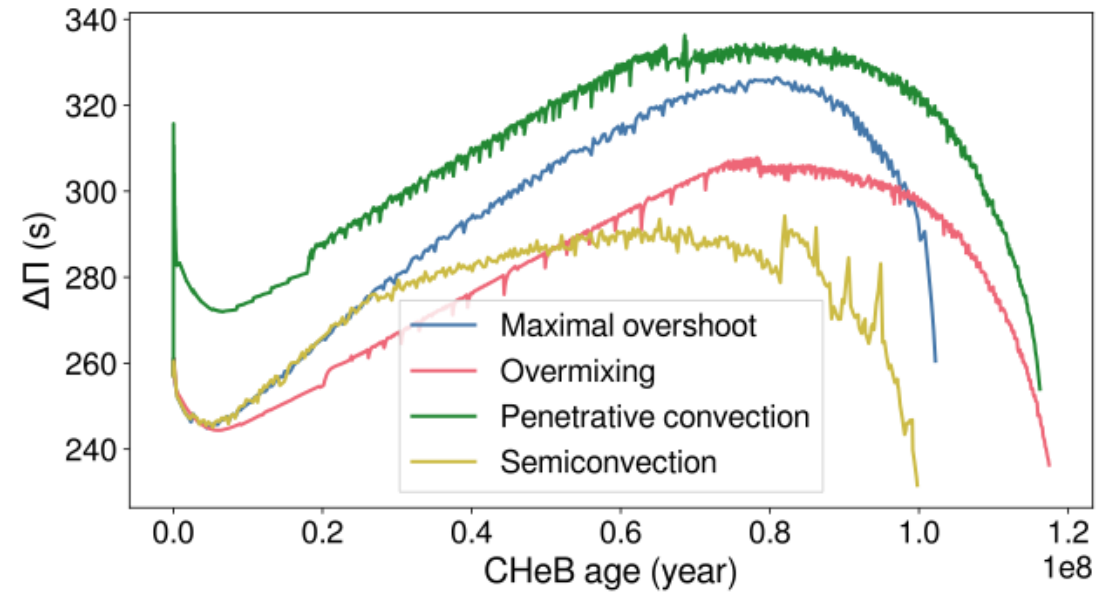
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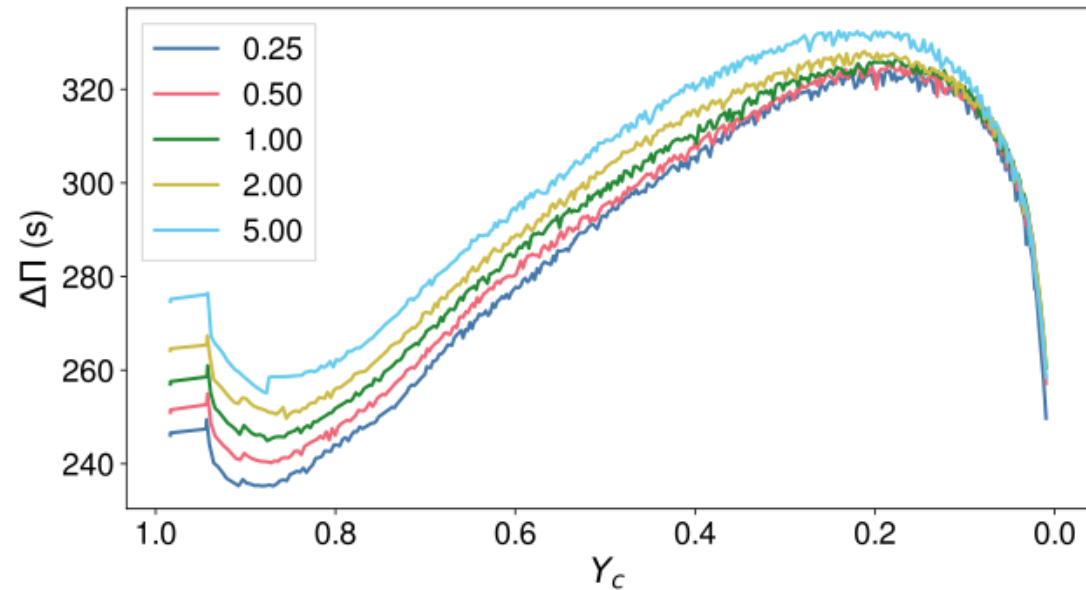
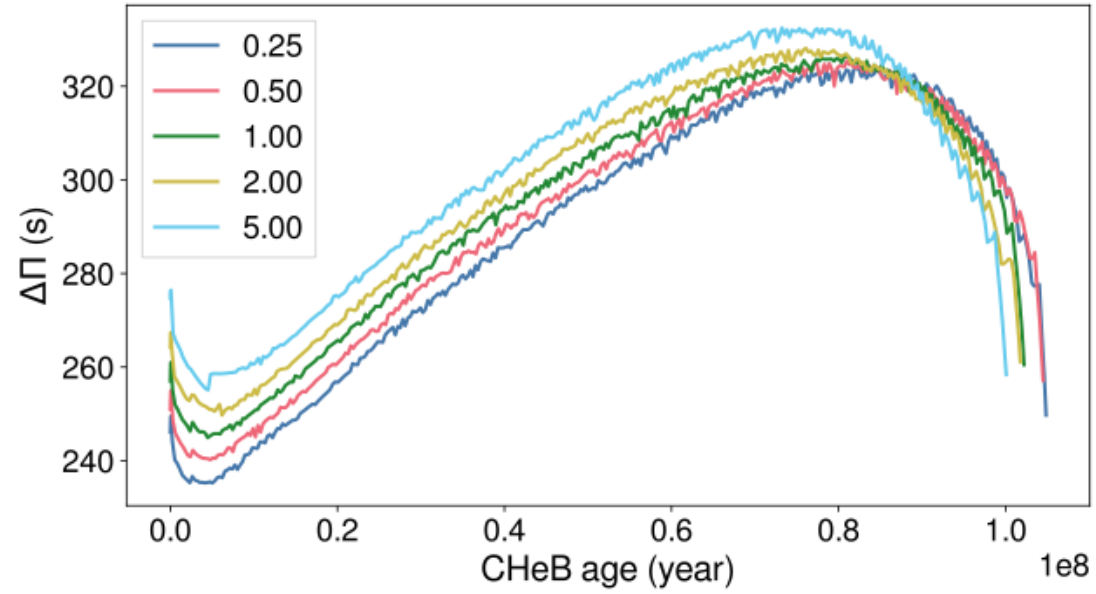
Core boundary mixing: Bruntt-Väisälä frequency



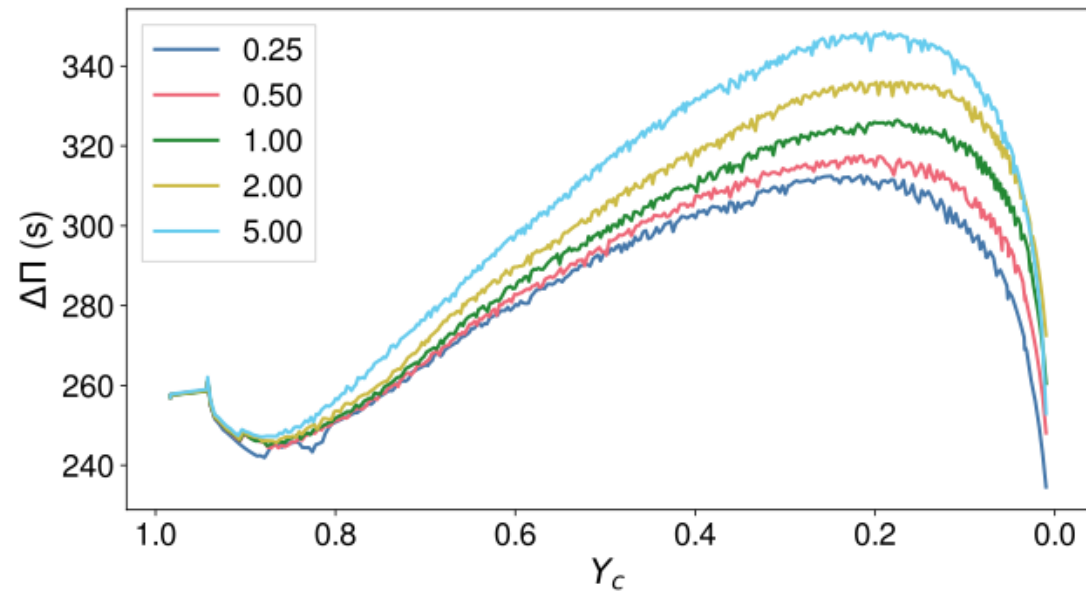
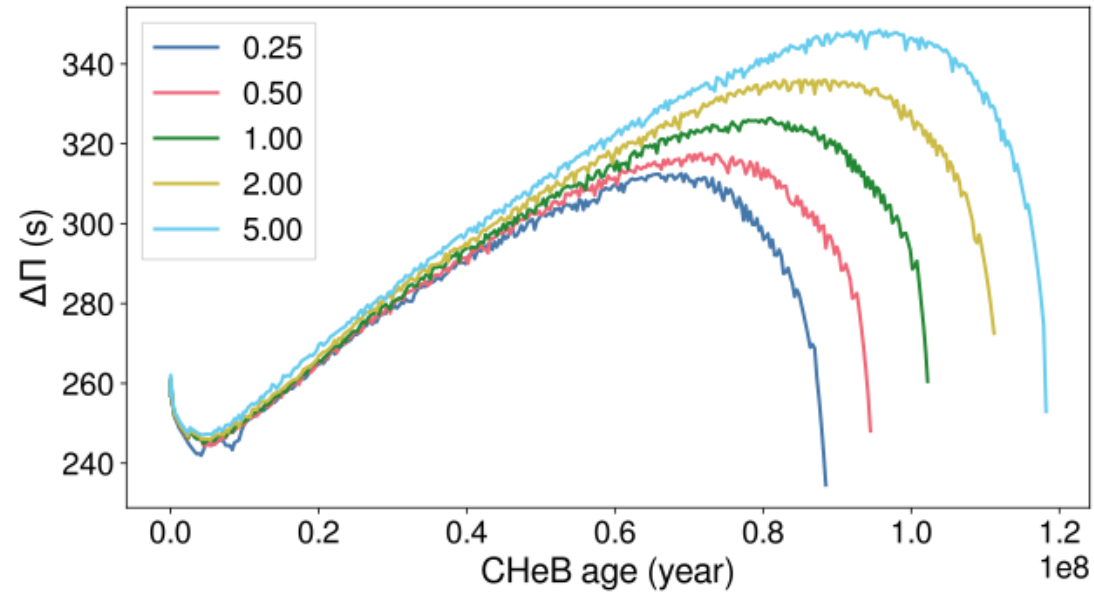
Effect of core boundary mixing on period spacing



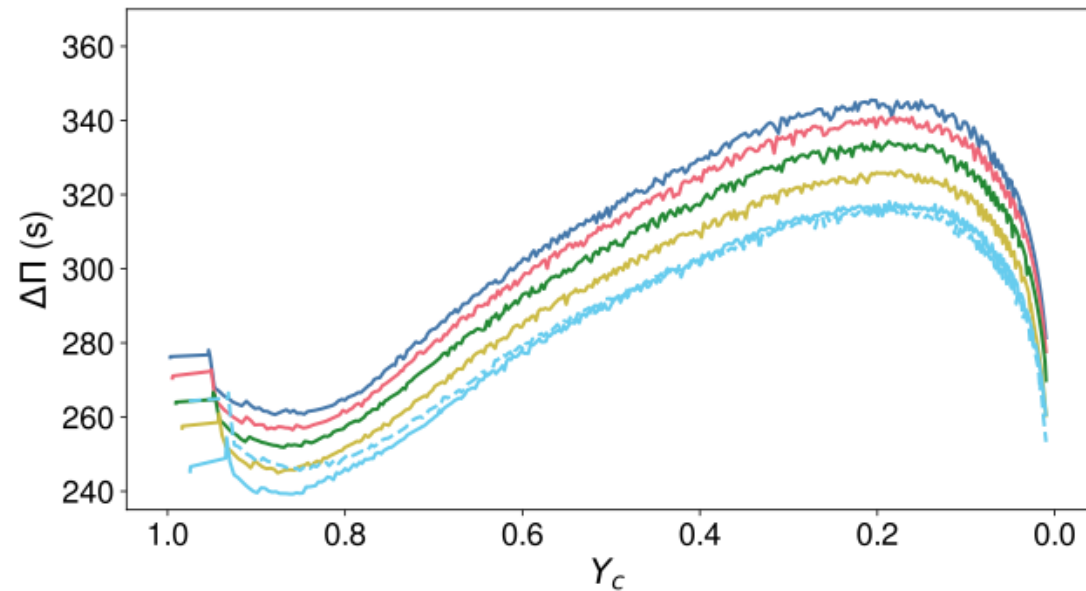
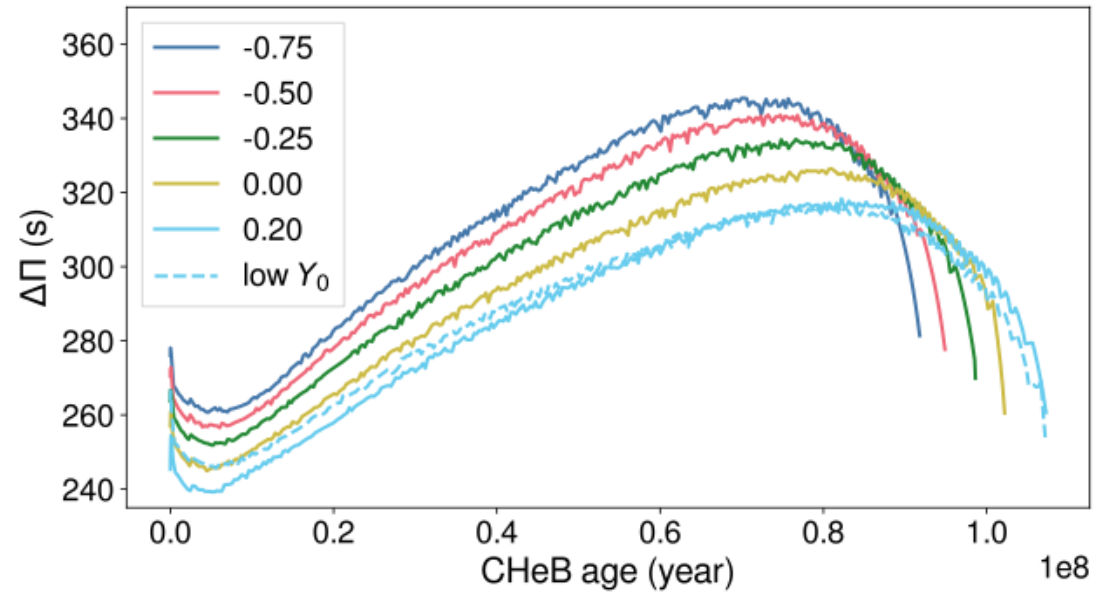
Nuclear reaction rates: 3α



Nuclear reaction rates: $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$



Nuclear reaction rates: [Fe/H]



After Lab slides

Cause of change in period spacing

- 3α :
 1. higher 3α -> He-flash @ lower T (earlier in the RGB) -> He-core less massive = smaller convective core -> lower period spacing
 2. higher 3α -> same L at lower ρ -> decreases local gravity -> decreases Brunt-Väisälä frequency -> higher period spacing

→ 2. dominates 1. leading to higher period spacings

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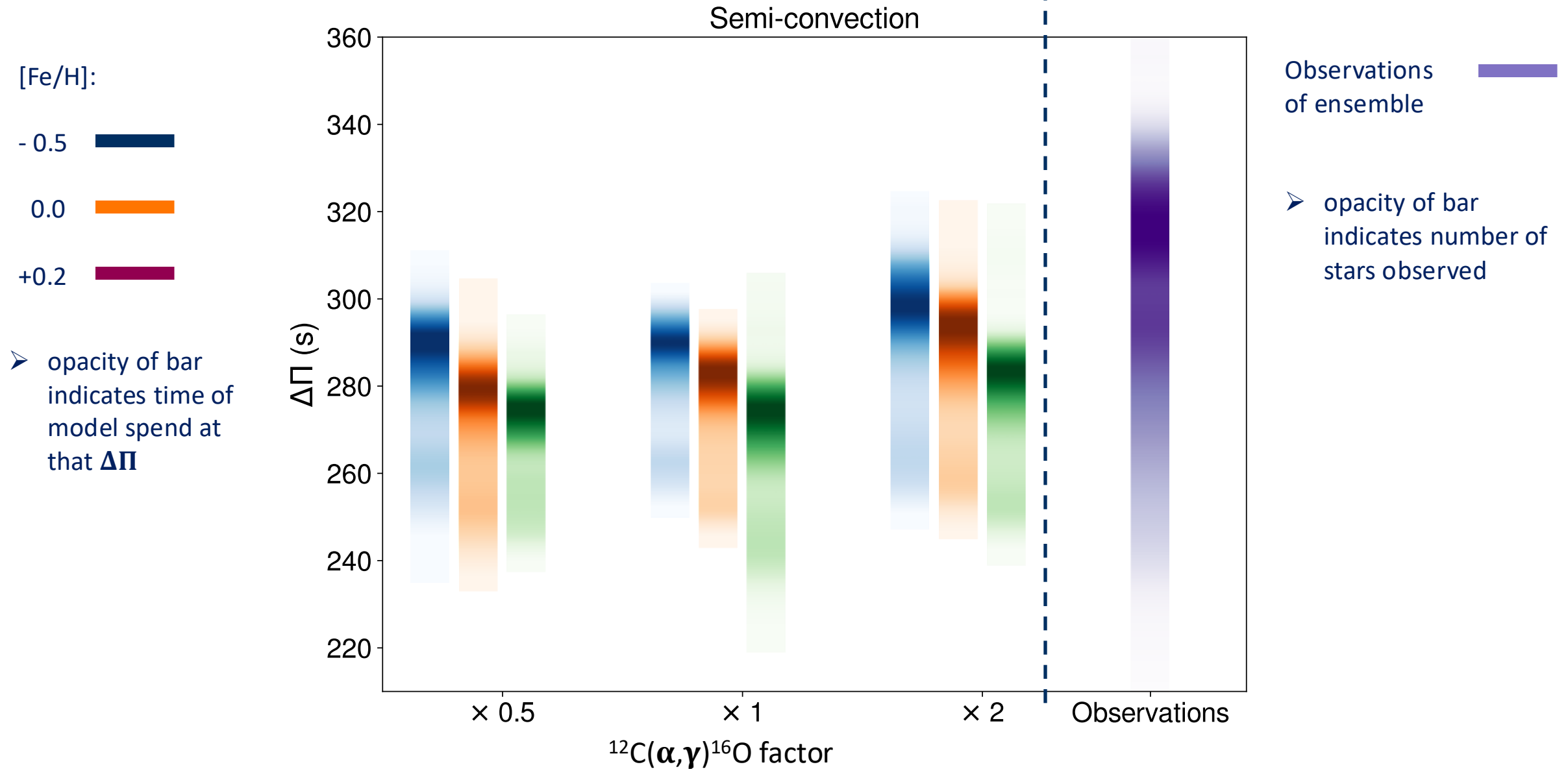
→ 2. dominates 1. leading to higher period spacings
- $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$:
 1. at early ages not much difference as $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ produces negligible part of L
 2. increasing $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ extends the CHeB phase -> during the CHeB phase the core expands -> higher period spacings

Cause of change in period spacing

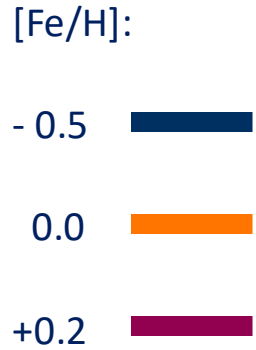
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- [Fe/H]:
 1. a metal poor star ignites He at a more massive core -> higher period spacing
 2. decreasing metallicity shortens CHeB phase

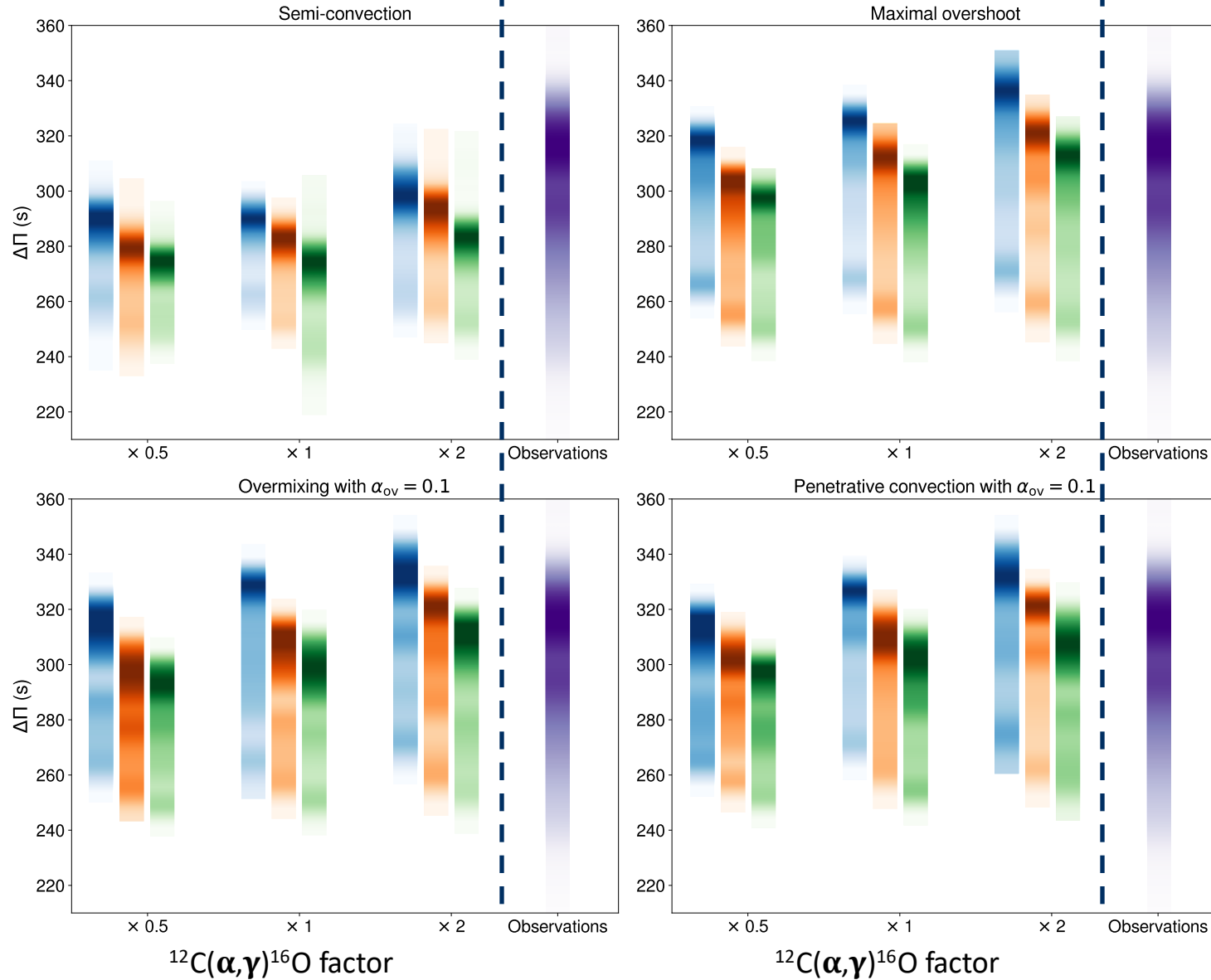
Combined effects: $3\alpha + {}^{12}\text{C}(\alpha, \gamma){}^{16}\text{O} + [\text{Fe}/\text{H}]$



Combined effects: $\text{CBM}_1 + 3\alpha + {}^{12}\text{C}(\alpha, \gamma){}^{16}\text{O} + [\text{Fe}/\text{H}]$



➤ opacity of bar indicates time of model spend at that $\Delta\Pi$



Observations 
of ensemble

➤ opacity of bar indicates number of stars observed